## FROM THEPROS

large-scale analysis of world-class solves reconstructions FIRST EPISODE-CFOP

## THE PEOPLE BEHIND THIS PROJECT

## The following analysis relies on the concerted effort of a number of people



Stuart Clark: the reconstruction god, single-handedly reconstructed more than a thousand of the solves that comprise the source data for this analysis; It is hard to render justice to the amount of effort (and speed) that went into reconstructing the solves whose features are synthesised here. Unable to stop there, Stuart was instrumental as a sparring partner in the analysis phase of this project

Gil Zussman: the creator of speedcubedb.com, which among its many features collects and present all the reconstructions; Besides creating many of the tools that make reconstructions possible today, Gil's contribution in providing both data and insights was an essential part of this work

- Basilio Noris: obsessed with data visualisation, he plunged into the raw data and made this analysis and document, extracting what could be of interest and could provide new learnings and spent way too much time making colourful charts

A special thanks to all the solvers who have contributed their solves, sometimes having to suffer through our pleas for ao50s and ao100s, days or weeks on end. Even if all your contributions have not borne fruit yet, they are at the heart of what it has been possible to do here. And a final thanks to the
Reconstruction Friends discord, which - besides fostering a culture of exchange and sharing - reunites most of the efforts of reconstruction that has allowed this analysis to exist. And a final thanks to Feliks, Phillip and Ben for reviewing this in its final phase of preparation


A tribute to the original Recon God While the vagaries of life sometimes force people to focus on new things, legacies remain Brest not only reconstructed more than 2000 solves on his own, he trained and made the current generation of reconstructors what it is

## HOW THIS DOCUMENT IS STRUCTURED

## THE ANALYSIS IN ITS DIFFERENT PARTS

. The Dataset: A quick overview of the data and its features (and flaws)

- Solve-level analysis: what can we learn from solves of the fastest solvers? What elements are common to all people, which seem peculiar to some but not all?
- CFOP: All we can learn about cross: are there common elements to efficient crosses (e.g. 2-3-4gen)? What about rotations? Do $x$ - and xxcrosses come with a certain frequency, and are they really worth it?
- CFOP: First two layers: is there a core of "frequent pairs" that get selected early in the solve (1 st/ 2nd slots)? What are the preferred inserts, and do they change significantly across solvers? Rotations vs fancy executions, is there a clear consensus?
- CFOP: Last layer: what can we learn from last layer execution? Are zbll algs worth the recognition slowdown? How often are skips happening? How much of that is due to influencing vs chance?
- Conclusions and moving forward: Many things remain to be done, least of which is tackling the other methods (Roux, I'm looking at you!)

A VERY SHORT CRASH COURSE ON DATA VISUALISATION


## A BIRD'S EYE VIEW ON THE DATA AT THE TIME OF WRITING



## THE DATASET IN NUMBERS



307 DISTRIBUTION OF SOLVE YEARS


Note: Excludes solves for which a date is not available (~47\%)

SOLVE TIME BY YEAR


## BIASES IN THE DATA, AND IN THE ANALYSIS



- Solves: partly by design a majority of the reconstructions here are very good (and maybe very lucky) solves. This means we are not always encapsulating what would happen with "great cubers, nasty scrambles", and whether specific strategies might work better than others on these.
Speedcuber-level analysis: we don't have the same amount of data from all speedcubers, for some we have 50 solves, for others 5, for a couple we have hundreds. This means that we sometimes only have a selection of the very best solves, rather than an overall understanding of the habits and solving particularities of the speedcubers themselves.
$3 \times 3$ AVERAGES FOR SPEEDCUBEDB SOLVERS

$3 \times 3$ SOLVE TIMES FOR /R/CUBERS SOLVERS (2020)



## A BIG BIAS IN THE AVAILABILITY OF DATA WILL FOCUS OUR ANALYSIS ON CFOP

DISTRIBUTION OF SOLVES BY METHOD


The eternal battle of the big 4, or big 2, or big whatever: When the database started, a focus was understandably put on the prevalent method, and on the fastest solves, which happened to coincide in the CFOP / Fridrich method. This is not to say that the other methods do not provide plenty of material for insightful understanding of what makes solving the cube possible, but we simply don't have enough data on those (yet) to obtain reliable results

This is why most of this analysis (for now) will revolve around the CFOP steps

## AND FINALLY A WORD OF CAUTION

"I do think world class F2L (and now even LL) is half art, half science though, and fingertricks/regrips are such a key element."

- Feliks Zemdegs


## So let's not take all of this too seriously!



UNSURPRISINGLY, THE FASTER THE SOLVE, THE LOWER THE MOVE COUNT AND THE FASTER THE TPS, BUT THE TWO DO NOT HAVE TO GO IN LOCKSTEP


GENERAL TPS BY SOLVE TIME


## TPS VS EFFICIENCY : THERE SEEMS TO BE A TRADE-OFF AFTER SOME POINT



```
Diminishing Above a certain TPS, solvers are
returns }\begin{array}{l}{\mathrm{ unable to ensure the same degree of}}\\{\mathrm{ efficiency to proportionally reduce}}
their times
```

Efficiency |The performance of slower
Gap $\begin{aligned} & \text { speedcubers is less a function } \\ & \text { of TPS, and more a lack of } \\ & \text { move efficiency }\end{aligned}$



## VERY DIFFERENT SPREADS IN THE NUMBER OF MOVES FOR DIFFERENT SOLVERS









## AT THE FASTEST LEVEL OF SOLVES, LAST LAYER SHRINKS (THANKS TO SKIPS), AND CROSS TAKES UP A BIT MORE OF THE SOLVE TIME (DUE TO XCROSSES)

TIME SPLITS SUB4 VS SUB10

PROGRESSION OF TIME SPLITS



## MOST SOLVES ARE BETWEEN 5 AND 7 GEN, WITH CROSS BEING THE MOST COMPLEX STEP

TOTAL SOLVE GEN


Average Gen:
6.1 gen

AVERAGE GEN BY SOLVE TIME


It's not really
the gen

Gen choice does not seem to be affecting times, with no difference between high vs low times (slightly lower for sub4, but not significantly so)

AVERAGE GEN PER STEP


## ROTATIONS VS GEN : NEVER ROTATE DURING CROSS, ALWAYS ROTATE FOR F2L!



## F2L TAKES UP THE LARGEST PART OF THE SOLVE TIME AND MOVE COUNT, BUT IS PERFORMED WITH PRETTY HIGH TPS,

 CROSS IS THE ONE THAT USES THE QUIRKIEST MOVES, AND IS PERFORMED AT A LOWER TPSCFOP STEP EXEC. TIME


CFOP STEP MOVE COUNT


CFOP STEP TPS


When they say it's all about f2I

The largest variation in CFOP solves comes down to f21: this is what makes or breaks a solve. However the other steps should not be discounted, as every bit helps (or hurts) the overall results

Planning is not muscle memory

Whilst cross can be planned during inspection, its execution is not a triggering of a memorised alg, as is the case of the following CFOP steps. Despite this, solvers are executing it at only $30 \%$ slower tps

## EVERYONE'S GOT MOVES, AND THEY ARE MOSTLY RU (SORRY S-SLICE CROWD!). CROSS IS THE MOST ECLECTIC STEP IN THE SOLVE

CFOP OVERALL MOVE USAGE


MOVE USAGE BY CFOP STEP


## SOME MOVES ARE BETTER THAN OTHERS FOR DIFFERENT STEPS: S SLICES LOOK GREAT FOR OLL, LESS SO FOR ANYTHING ELSE



STEP EXECUTION TIME BY TYPE OF MOVE IT USES


If it's not
one it will
have to be the other

Unsurprisingly, there is a very strong negative correlation between Righty and Lefty moves, as well as (to a lower extent) R vs M moves: they serve similar purposes, but solvers who prefer one will use the others less

The Zoomer generation

Usage of S and E slices, as well as f move (e.g.) inserts are positively correlated. The recent hike in popularity of these moves seems to have brought all of them to the fore at the same time

## M MOVES : A BIT BETTER THAN ONE AND A HALF OUTER-LAYER TURNS



Why only these PLLs

By sticking to the same PLLs we control for alg recognition complexity, which would make a comparison of the simpler EPLLs and other PLLS unfair towards outer-layer-based algs

But what about Roux?

The current analysis utilises a strictly comparable regime of algs, where the "thinking" component has been taken out of the equation (same PLLs, just different algs). But what about Roux? We know that the tradeoff between lower-move count and lowertps is present, but how much of it is due to Slice moves?

## WHAT ABOUT WORLD-RECORD LEVEL SOLVES?

9 WR AND SUB-WR SOLVES AT A GLANCE


## CROSS <br> Cross: xcross: xxcross: <br> 56\% 22\% 22\%

## What is world-record level

At the time of writing the current official $3 \times 3$ single WR
stands at $\mathbf{3 . 4 7 s}$ by Yusheng Du, for whom a number of
solves (including his WR) are part of our data.
However, multiple solvers have managed to get faster solves in unofficial venues, some on cam, others
reconstructed, some on stackmat, others on keyboard or smart cube.

Regardless, it is interesting to understand what it takes to get times as fast as the (current) world record


## CHAPTER 2 : CROSS

## A CROSS IS USUALLY DONE IN 6 MOVES, AT 5.2 TPS, WITH 1 ROTATION

## Cross Stats



## CROSS COLOR : EVEN AT THESE LEVELS, WHITE AND YELLOW COME OUT ON TOP (BY A FACTOR OF 2 EACH RESPECTIVELY)





MEDIAN SOLVE TIME BY CROSS COLOR


| Or not | Or is it just the least <br> seeing it <br> frequent color, and <br> therefore we don't have |
| ---: | :--- |
| enough? | enough bad solves? |

Seeing red $\left\lvert\, \begin{aligned} & \text { Is there something intrinsically "better" with red cross that } \\ & \text { makes it slightly faster than the other colors, or is that a fluke? } \\ & \text { Might physiological adaptations to contrast recognition } \\ & \text { relating to red be at play here? We need to dig deeper. }\end{aligned}\right.$

## BUT WHEN WE LOOK ON A SOLVER BY SOLVER BASIS, THE STORY CHANGES

## AVERAGE SOLVE TIME BY CROSS COLOR



AVERAGE OF ALL SOLVERS EXCEPT THOSE FOR WHOM WE HAVE 80+ SOLVES


## X \& XX CROSSES ARE RELATIVELY FREQUENT IN GENERAL (ALMOST $\mathbf{1 / 5}$ SOLVES OVERALL), BUT THEY BECOME

 CRUCIAL FOR THE FASTEST SOLVES; PSEUDO AND PARTIAL SEEM TO BE MORE NICHE AND NOT AS ESSENTIAL


Everything | The faster the solve, the more likely it started out starts with a good start
with a complex (and efficient) $X(X)$ cross solution Maybe it's not a required condition, but it looks ike something worth working towards

## X \& XX CROSSES ARE RELATIVELY FREQUENT IN GENERAL (ALMOST $1 / 4$ SOLVES OVERALL), BUT THEY BECOME

 CRUCIAL FOR THE FASTEST SOLVES; PSEUDO AND PARTIAL SEEM TO BE MORE NICHE AND NOT AS ESSENTIAL


Tradeoffs
XXCross can shave more than 0.5 seconds on a solve, this explains why they appear so often in good solves


## 1/3 OF SOLVES HAVE NO ROTATIONS OR WIDE ROTATIONS IN CROSS, BUT THE FASTEST SOLVES HAVE FEW




TOTAL ROTATIONS BY SOLVE TIME Rotations + wide moves

\# OF WIDE MOVES DURING CROSS



CHAPTER 3 : FIRST 2 LAYERS

F2L PAIRS TAKE 8 MOVES ON AVERAGE, BUT TO GO FASTER THIS NEEDS TO GO DOWN (AND THE SOLVE NEEDS TO LET YOU DO IT!)


FIRST PAIR TENDS TO BE FASTER (THE POWER OF CROSS +1), THE OTHER PAIRS ARE VERY COMPARABLE; IN TERMS OF MOVE-COUNT, 8 IS THE GENERAL RULE


Cross+1
and
First pair ends up being $18 \%$ faster than the other pairs (on average), the effect of inspection, or the choice of "easy planning pickings" at the beginning of the solve


A case of good cases

The typical move count is basically the same for all pairs (8), but the advantage of picking an "obvious pair" shows the higher occurrences of short first pairs


1 ST SLOT ENDS UP IN THE BACK-RIGHT THE MOST OFTEN, AND THE FASTER THE SOLVE, THE MORE LIKELY IT STARTS THERE. LAST SLOT ENDS FRONT-RIGHT HALF OF THE TIME


Left Out
Overall for any of the pairs, the left slots comprise less than $40 \%$ of slot usage, which means that solvers prefer to fill in on the right and cube rotate rather than go mess with left slots


## STANDARD INSERTS ARE THE WAY TO GO THE VAST MAJORITY OF TIME, SLEDGE IS USED A BIT MORE ON LAST SLOT, BUT IT REMAINS VERY RARE



PREVALENCE OF DIFFERENT TYPES OF INSERTIONS



20 MOST FREQUENT INSERTS


## DIFFERENT SOLVERS, SLIGHTLY DIFFERENT PREFERENCES

MOST USED INSERTS


## THE INSERT METHOD DOES NOT INFLUENCE THE EXECUTION TIME MUCH, BUT WIDE MOVES AND SLICES DO NOT SEEM TO BE A GOOD IDEA FOR F2L



〇ㅇํㄱㄴ PAIR TIME BY MOVE USED
Qْ Q TPS BY MOVE USED


## THE TYPICAL F2L HAS 2-3 ROTATIONS, FIRST PAIR IS THE LEAST LIKELY TO NEED ROTATIONS, AND THE FASTER THE SOLVE, THE FEWER THE ROTATIONS

TOTAL ROTATIONS DURING F2L


F2L PAIRS WITH NO ROTATIONS


TOTAL F2L ROTATIONS BY SOLVE TIME


## COMBO F2L PAIRS : VERY INFREQUENT, BUT THE TIME-SAVES ARE DISCONCERTINGLY

 HIGH : IS THIS SOMETHING MOST SOLVERS ARE NOT ABLE TO DO?SOLVE TYPE WITH AND
WITHOUT COMBO PAIRS


Is there a | The difference in solve time cannot be attributed to |
| :--- | :--- | skill bias?

the time-save of skipping a pair alone: might it be that only the fastest solvers manage to do combos on the fly well?

OCCURRENCES OF F2L
PAIRS SOLVED TOGETHER


## THE KINGS OF PAIR COMBOS : SOME DON'T GAIN A LOT, BUT OTHERS SAVE UP TO 13\% OF THE ENTIRE SOLVE

SOLVERS OF F2L PAIR COMBOS
for which we have at $4+$ solves with combo pairs and $50+$ solves total


$$
\begin{aligned}
& \text { AVERAGE GAIN } \\
& \text { (weighed average) }
\end{aligned}
$$





## LAST LAYER IS WHERE A LOT OF THE WORK OF SOLVE OPTIMISATION (OR LUCK) COMES INTO PLAY



SUB4 SOLVES


SUB10 SOLVES


## SOME BIG DISPARITIES ACROSS OLLS, WITH THE SLOWEST ONES 2.5X SLOWER THAN THE FASTEST

\%FREQUENCY OF OLL CASES

O. OLL EXECUTION TIME BY OXCludes ZBLL. OLLLP Skips $\operatorname{OLL}$ CASE Excludes ZBLL, OLLCP, Skips


FAST AND FURIOUS 57
5 fastest OLL in live solves


OLL 27


OLL 45


OLL 44


OLL 33


OLL 26


APOCALYPSE NOW $\mathbf{5}$ slowest OLL in live solves


OLL 53


OLL 56

## DOT OLLS GET A LOT OF FLAK, AND SOME OF IT IS DESERVED. BUT IS IT WORTH TRYING TO DO SOMETHING TO AVOID THEM? NOT REALLY

TOTAL SOLVE TIME BY OLL TYPE
Sub10 solves only, incl. skips


OLL EXECUTION TIME Excluding ZBLL/OLLCP/skips


LAST PAIR EXECUTION TIME
Sub10 solves only


Median time loss for Dot OLL
0.16 sec

Minimum time loss for Last slot manipulation
© 0.27 sec

## SOME PLLS ARE BORN MORE EQUAL THAN THE OTHERS

\%FREQUENCY OF PLL PERM OCCURRENCES



You shall not pass!

Acknowledging that they don't happen often anyway, it is looks like it is not possible for some PLL to be part of a sub4 solve. When looking at the median solve for the different cases, however, the picture is much more mixed, with Y-perm, of all things, coming out on top.

The chicken and the egg

What this data shows is not that solvers are able to influence PLL to the tune of $2 x$, (although this is also partly the case, especially for EPLL), rather, that it is difficult for a solve to be "good enough" to end up in this database when it had, e.g. a $\vee$ perm compared to a Jb perm.

## WHAT ABOUT THE FASTEST SOLVES?



FREQUENCY OF PLL PERM OCCURRENCES 5-7s solves only, Excluding PLL skips and wonky last layers


Note: 5-7sec solves without a PLL skip: 73\%


Note: Sub5 solves without a PLL skip: 36\%

[^0]PLL FREQUENCY OCCURRENCES

## PLL EXECUTION : 1.51 SEC ON AVERAGE, SOMETIMES LESS SOMETIMES MORE

EXECUTION TIME BY PLL TYPE



OLLCP + EPLL IS AT BEST SIMILAR TO OLL+PLL (A PER-SOLVER ANALYSIS SHOWS OLLCP TO BE USUALLY SLOWER THAN OLL EVEN WHEN SKIPS ARE INCLUDED); COLL DOESN'T SEEM TO BE WORTH IT


## ONE IN FIVE SOLVES ENDS UP IN A SKIPS, WHICH ARE INFLUENCED ALMOST HALF OF THE TIME; A SKIP,

 ON AVERAGE, SAVES 1.1 SECONDS, WITH PLL BEING VERY SLIGHTLY MORE TIME-SAVING THAN OLLPREVALENCE OF LAST LAYER SKIPS


LAST LAYER INFLUENCING
SOLVE TIME BY TYPE OF SKIP


A biased sample, by necessity

The selection of "good solves" in the dataset, skews the sample significantly compared to a random solve. However, the fact that such a high rate of skips are influenced by the solver tells us that these are important components of the best solves

## UNSURPRISINGLY, LUCK PLAYS A VERY KEY ROLE FOR THE FASTEST SOLVES; BUT INFLUENCING HAPPENS A LOT, (AND DIFFERENTLY FOR DIFFERENT SOLVERS)



## THE MAJORITY OF LAST LAYER ALGS REQUIRE SOME ADJUSTMENT, WITH OLL

 REQUIRING THE MOST: SOLVERS LEARN ALTERNATIVE ALGS FOR MULTIPLE PLL ANGLES

AUF BEFORE AND AFTER EXECUTION OF LAST LAYER ALGS


AUF EXECUTION TIME


Death by a
At the level of the fastest solve, a 0.2 sec loss due to AUFs still accounts for $5-7 \%$ of the entire solve. not an entirely negligible question therefore whether to strategise around AUF when choosing an alg
thousand cuts
cuts


Average LL:
1.77 AUFs

## EVERY BIT HELPS FOR THE FASTEST SOLVES : NO-AUFS ARE TWICE AS

 LIKELY TO OCCUR IN SUB4 SOLVES

AUFS BY SOLVE TIME
for <4, 4-5, 5-6, 6-7, 7-8 second solves

\% OF AUFS AT END OF SOLVE


## 侖 <br> CONCLUSIONS AND LEARNINGS

## WHAT CAN WE LEARN FROM ALL OF THIS

## SOME MORE AND SOME LESS SURPRISING FACTS

- At the fastest speeds, there is a tradeoff between TPS and move efficiency
- It might not be possible to be efficient if things are moving too fast
- The "canon" split for CFOP steps sits at around 16\% | 45\% | 17\% | 22\%
- For the fastest solves, last layer shrinks (skips), and cross goes up (x(x)crosses)
- X- and XX-crosses become a necessity for most of the fastest solves
- They appear in half of sub4 solves and appear in $\sim 20 \%$ of solves on average
- The vast majority of time standard RUR'-like inserts are good enough
- It's an even $\sim 50 / 50$ between joint and split pairs
- Sledge inserts are very rare (a bit more frequent for last pair, at 6\%)
- Slice moves are a bad idea during F2L, f-move inserts are quite good though
- S moves are quite good in OLL, but not so much anywhere else, although that might be because we don't have good algs yet!
- Never rotate for cross, always rotate for f2l
- The time loss due to rotation is important in cross but negligible in f2l, and more than compensated by the gain in speed by keeping the moveset simpler
- Last Layer skips happen $20 \%$ of the time, and solvers are influencing them $\sim 50 \%$ of the time
- But the fastest solves have a lot fewer forced skips: it is probably time consuming to think about them at those speeds. Is it better to simply play and pray?
- AUFs are needed 60\% of the time
- AUFs are less frequent in the faster solves, with that extra bit of luck contributing to the overall "shaving time bit by bit" trend that seems to describe in general the fastest solves
"Keep it simple" seems to be the winning strategy for the fastest CFOP solves


## WHAT'S NEXT FOR THIS ANALYSIS

## - The other methods

- A recent spurt of efforts has been made into recording and reconstructing Roux solves. Despite this, the data available is still limited. The next challenge is to integrate the existing data into the scab and then conduct a similar analysis on the second of the Big 2
- Other traditional methods (ZZ, Petrus) have not seen a lot of usage, despite its coterie of stalwart defenders. While I suspect that a large-scale analysis such as the one we present here and the one planned for Roux will not be feasible, many things can still be learnt about these methods
- Much more recent methods (Mehta), somewhat boutique (zipper) or meme-but-not-only methods (Belt!) can present nuances in solving strategies that might be interesting. A number of awesome people have already or are in the process of contributing sizeable amounts of solves for these methods, so the only barrier left is to put together the analysis itself!


## - Further analysis

- Currently all solves are taken together, but given the prevalence of low-solve-count solvers in the data, many KPIs are not encapsulating the variance within solver, and the number of solvers for which we have sufficient solves is (for now) relatively low. This is definitely one area where we'll be working to improve the analysis!
- Analysis of specific steps in the methods (e.g. F2L inserts, choice of PLL all for specific cases) is for now surface level. Getting smarter tools to identify patterns in the solves and how they influence the outcome is likely to prove a challenging but rewarding endeavour


[^0]:    The case of
    While not necessarily a PB killer, some perms simply disappear from the fastest solves, That said it is worth remembering that $2 / 3$ of sub5 solves
    end with a PLL or LL skip the lost perms

